# Co-optimization of Multiple Relevance Metrics in Web Search

Dong Wang[1,2,*], Chenguang Zhu[1,2,*], Weizhu Chen[2], Gang Wang[2], Zheng Chen[2]

[1]Institute for Theoretical
Computer Science
Tsinghua University
Beijing, China, 100084
{wd890415, zcg.cs60}@gmail.com

[2]Microsoft Research Asia
No. 49 Zhichun Road
Haidian District
Beijing, China, 100080
{v-dongmw, v-chezhu, wzchen, gawa,
zhengc}@microsoft.com

## ABSTRACT

Several relevance metrics, such as NDCG, precision and pSkip, are proposed to measure search relevance, where different metrics try to characterize search relevance from different perspectives. Yet we empirically find that the direct optimization of one metric cannot always achieve the optimal ranking of another metric. In this paper, we propose two novel relevance optimization approaches, which take different metrics into a global consideration where the objective is to achieve an ideal tradeoff between different metrics. To achieve this objective, we propose to co-optimize multiple relevance metrics and show their effectiveness.

## Categories and Subject Descriptors

H.3.3 [**Information Systems**]: Information Search and Retrieval;

## General Terms

Algorithms, Design, Experimentation, Theory.

## Keywords

Learning to Rank, User Feedback, LambdaRank.

## 1. INTRODUCTION

Recent advances in search relevance have positioned it as a very important aspect of information retrieval (IR), and traditional works to improve search relevance can be grouped into two different categories based on the kinds of metrics used for optimization. The first one aims to improve relevance from explicitly judged labeled data by learning a ranking model to optimize a metric, like NDCG [4]. We call this kind of metric an explicit relevance metric since it's based on the explicit data. The other category looks for ways to improve search relevance by leveraging large-scale implicit user behavior log data from commercial search engines, and optimize another kind of metric, like CTR [2], pSkip [5]. We call this kind of metric an implicit relevance metric since it's based on implicit data.

However, to the best of our knowledge, previous works mostly focus on optimizing one metric to improve search relevance, though both the explicit relevance metric and implicit metric have their own merits [3]. Yet, we empirically observe that the exclusive optimization of one metric cannot always achieve the optimal ranking of another metric. For example, directly optimizing NDCG on the explicit data often results in a non-optimal relevance for pSkip on the implicit data, and vice versa. We may see this conflict from a lot of real examples. As an instance, for a query $q$, we will only consider its three URLs: $u_1$, $u_2$ and $u_3$. For a case that $u_1$ and $u_2$ are both rated as Excellent while $u_2$ has a higher click frequency than $u_1$, if we only optimize NDCG, the NDCG is maximized if we put $u_1 > u_2$, where $>$ means the right part is put below the left part in the search result; however, the pSkip doesn't achieve the optimal result since we put $u_2$ with higher click frequency below $u_1$. In this extreme case, if we can optimize NDCG and pSkip simultaneously, we may put $u_2 > u_1$, so NDCG and pSkip can both achieve the optimal result. For another case: $u_2$ is a duplicate of $u_1$, so most users won't click $u_2$ and will likely jump to $u_3$ if they are unsatisfied with $u_1$. So if $u_1$ and $u_2$ are more relevant than $u_3$, maximizing NDCG will rank them as $u_1 > u_2 > u_3$, while optimizing pSkip will rank them as $u_1 > u_3 > u_2$ based on the click frequency. All of these real cases illustrate that we cannot solve this kind of conflict if we only consider one metric in optimization. Conversely, if we can take both metrics into consideration, it's possible for us to find an ideal tradeoff to optimize both metrics simultaneously.

In this paper, we propose to co-optimize the explicit relevance metric and implicit relevance metric simultaneously with our objective being to find an ideal co-optimization approach. Especially, we aim to answer the question: how can we maximize one metric without even slightly sacrificing another metric? For example, we aim to find a ranking function that optimizes pSkip with the constraint that the decrease of the NDCG score is less than 0.1 percent. To achieve this objective, we propose two novel methods from different machine learning approaches to co-optimize multiple relevancies.

## 2. LEARNING MODELS

Exclusive optimization for explicit metric cannot always achieve the optimal value for implicit metric, and verse vice. Here we propose two combination models.

## 2.1 Indirect Optimization Model

Firstly, we propose *indirect optimization model*. In this model, we try to integrate CTR into the calculation of NDCG. In order

to balance two measurements, we add a tradeoff parameter $\alpha$ into our optimization function as (1):

$$f_{IO} = \frac{1}{f_{max}} \sum_i \frac{2^{r_q(i)} \cdot \left(\alpha CTR\left(d_q(i)\right) + 1 - \alpha\right)}{log\,(1+i)} \quad (1)$$

where $f_{max}$ is the normalizing factor being the ideal evaluation score, $r_{q(i)}$ is the rating for document ranked at position $i$. $CTR\left(d_q(i)\right)$ is the click through rate for document ranked at position $i$. Here, we use LambdaRank[1] to optimize the evaluation function. The $\lambda_{ij}$ here is as (2):

$$\lambda_{ij}^{f_{IO}} \equiv S_{ij} \left|\Delta f_{IO\,ij} \frac{\partial C}{\partial o_{i,j}}\right| \quad (2)$$

Here $S_{ij}$ equals 1 when $d_q(i)$ is more valuable than $d_q(j)$ and -1 otherwise.

## 2.2 Direct Optimization Model

Moreover, we propose *direct optimization model*. For direct optimization we built the optimization function as (3):

$$f_{DO} = \alpha f + (1 - \alpha) NDCG \quad (3)$$

Here $f$ is an implicit evaluation function like CTR or pSkip. We can generate two $\lambda$-gradients for each pair of training documents during the training process. One is generated by document's label in order to optimize NDCG and the other is generated by user implicit feedback in order to optimize $f$. So that the total $\lambda$-gradient for each pair of search result is (4):

$$\lambda_{ij} \equiv \alpha \lambda_{ij}^f + (1 - \alpha) \lambda_{ij}^{NDCG} \quad (4)$$

More specially, $\lambda_{ij}$ for optimize NDCG and $f_{pSkip}$ is as (5):

$$\lambda_{ij} \equiv \alpha S_{ij} \left|\Delta f_{pSkip\,ij} \frac{\partial C}{\partial o_{i,j}}\right| + (1 - \alpha) S'_{ij} \left|\Delta NDCG_{ij} \frac{\partial C}{\partial o_{i,j}}\right| (5)$$

And $\lambda_{ij}$ for optimize NDCG and $f_{CTR}$ as (6):

$$\lambda_{ij} \equiv \alpha S_{ij} \left|\Delta f_{CTR@p\,ij} \frac{\partial C}{\partial o_{i,j}}\right| + (1 - \alpha) S'_{ij} \left|\Delta NDCG_{ij} \frac{\partial C}{\partial o_{i,j}}\right| (6)$$

Notice that $S_{ij}$ and $S'_{ij}$ may be different since they get their value by different evaluation function.

## 3. EXPERIMENTAL RESULTS

We set two experiments to show the performance of our learning models. More specifically, our experiments show that we can improve implicit relevance such as CTR, pSkip with explicit relevance NDCG no significant drop, and vice versa. We compare different learning models on a large real dataset. In the following diagram, **IO:** Stand for *indirect optimization model.* **DO:** Stand for *direct optimization model.*
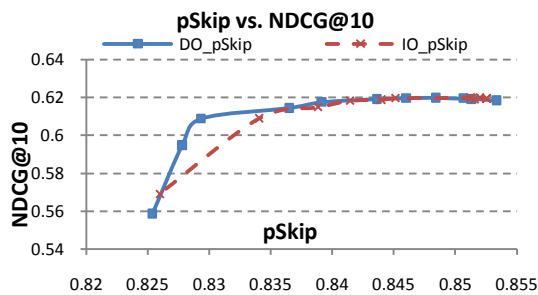


**Figure 1: curve generated by pSkip and NDCG@10**

In Figure 1, we show the performance of *direct optimization model* and *indirect optimization model* are almost the same when pSkip is high, but *direct optimization model* will get a higher NDCG score when pSkip score is low. Moreover, we get the same NDCG score and decrease pSkip score by 2% in our new learning models.
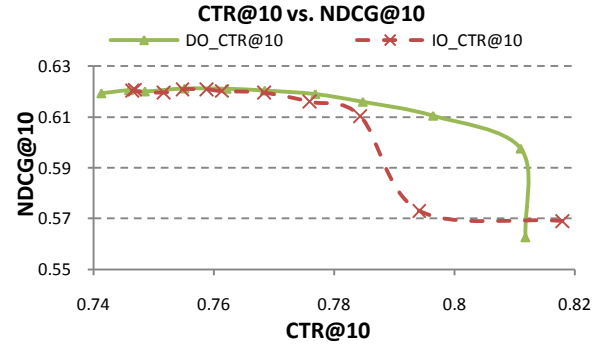


**Figure 2: curve generated by CTR@10 and NDCG@10**

In Figure 2, we show the performance of combing $f_{CTR@10}$ with NDCG by our learning models. We see *indirect optimization model* is more sensitive than *direct optimization model*. Both two models increase CTR score by 4% with NDCG score remains the same.

Overall, *Indirect optimization model* always treat explicit relevance as important metric. *Direct optimization model* can achieve the optimal point for any tradeoff parameter.

## 4. CONCLUSION

In this paper we investigate two novel approaches to co-optimize implicit relevance metric and explicit relevance metric, and evaluate our learning models' performance by the curve generated by NDCG, CTR and pSkip as entity metrics. By optimizing the combination function of these metrics, we can reach an ideal balance between explicit relevance metric and implicit metric. Especially, we achieve a better pSkip or CTR score without drop of NDCG score.

## 5. REFERENCES

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